

Enabling High Resolution Computed Tomography Neural Representation Using Batched Rays Sampling

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Introduction and Motivation

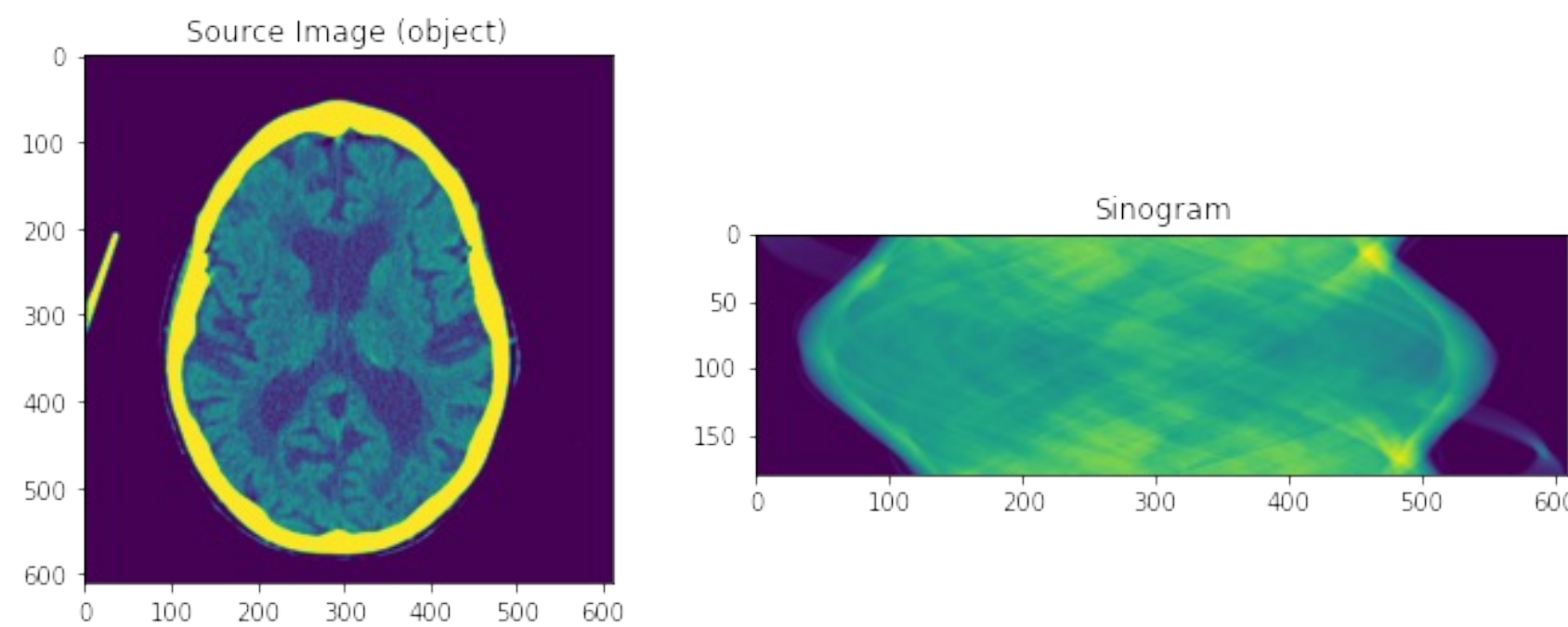


Figure 1. A CT of a brain (left), and its sinogram from 180 projections (right).

- Implicit neural representations (INR) have been at the frontier of the computed tomography (CT) reconstruction field.
- Those neural representations require large amounts of GPU memory to be trained, limiting their usage and accessibility.
- We propose a new approach to breaking down the ground truth to enable higher-resolution CT using smaller GPUs. (Figure 4)

Method

- We considered the conventional inverse radon transform as our baseline method for reconstruction. (Figure 2)
- The inverse Radon transform, however, conventionally reconstructs the whole image, which makes it memory expensive when fitting it to a neural network. (Figure 3)
- We proposed a method to break down the inverse Radon transform into single rays. (Figure 4)
- Each pixel in the sinogram space represents a ray (a vector of pixels) in the image space.
- We computed the associated vectors of pixels with every single sinogram pixel and stored them in a dictionary-like data structure.
- While training the network, we could fit as low as one sinogram pixel as our ground truth enabling the training on smaller GPUs.

Inverse Radon Transform

- Radon Transform (Eq1)

$$F(\alpha, s) = \int_{-\infty}^{\infty} f(t \sin \alpha + s \cos \alpha, -t \cos \alpha + s \sin \alpha) dt$$

- Inverse Radon Transform (Eq2)

$$f(x, y) = \int_0^{2\pi} F(\alpha, x \cos \alpha + y \sin \alpha) d\alpha$$

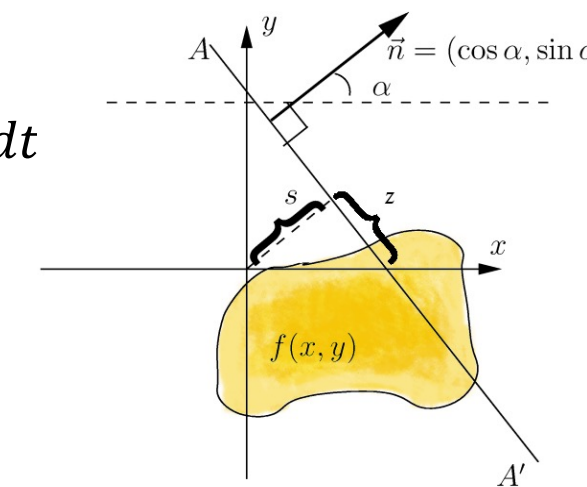


Figure 2. Radon transform. Maps f on the (x, y) domain to Rf on the (α, s) domain.²

Proposed Pipeline

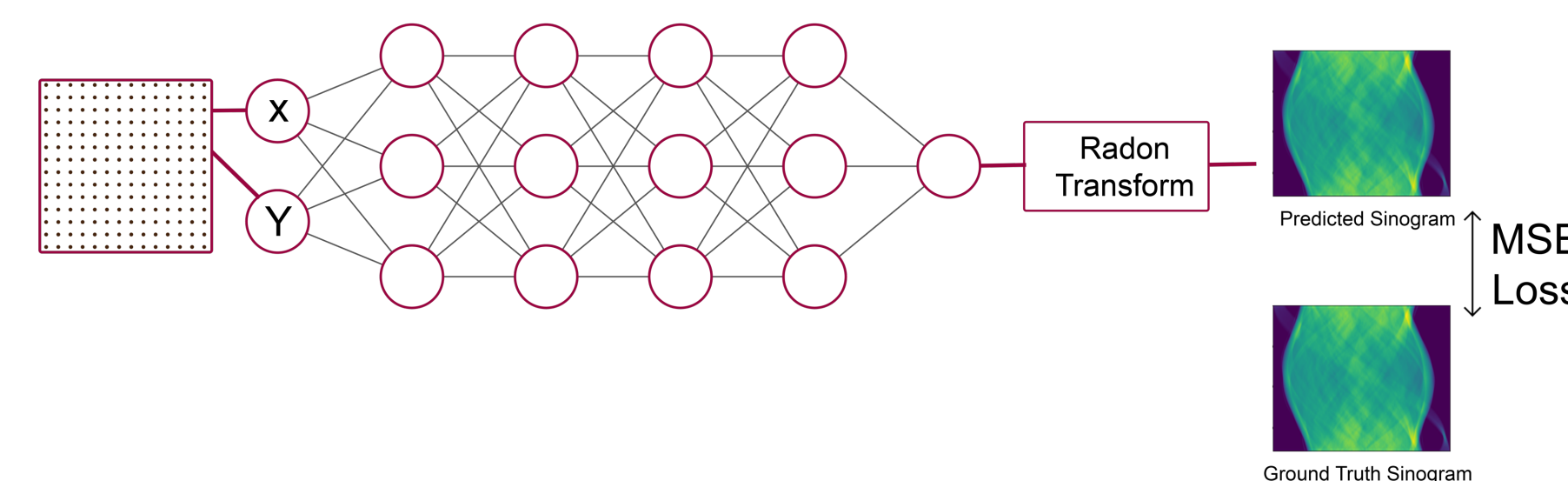


Figure 3. Traditional implicit neural network for computed tomography. Input: 50% of the coordinates of the desired CT image.

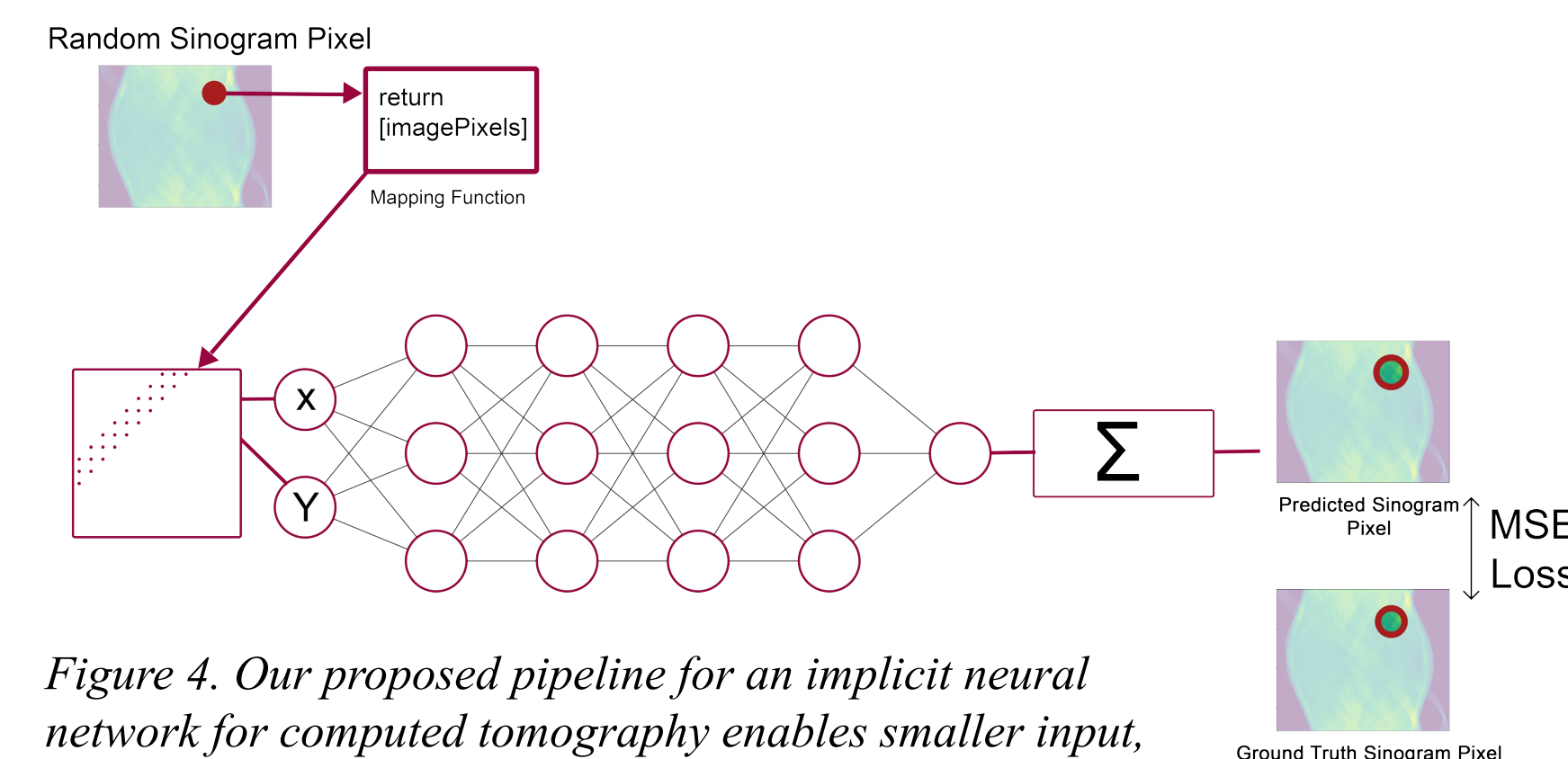


Figure 4. Our proposed pipeline for an implicit neural network for computed tomography enables smaller input, and therefore less memory. Which in return enables fitting higher resolution CT.

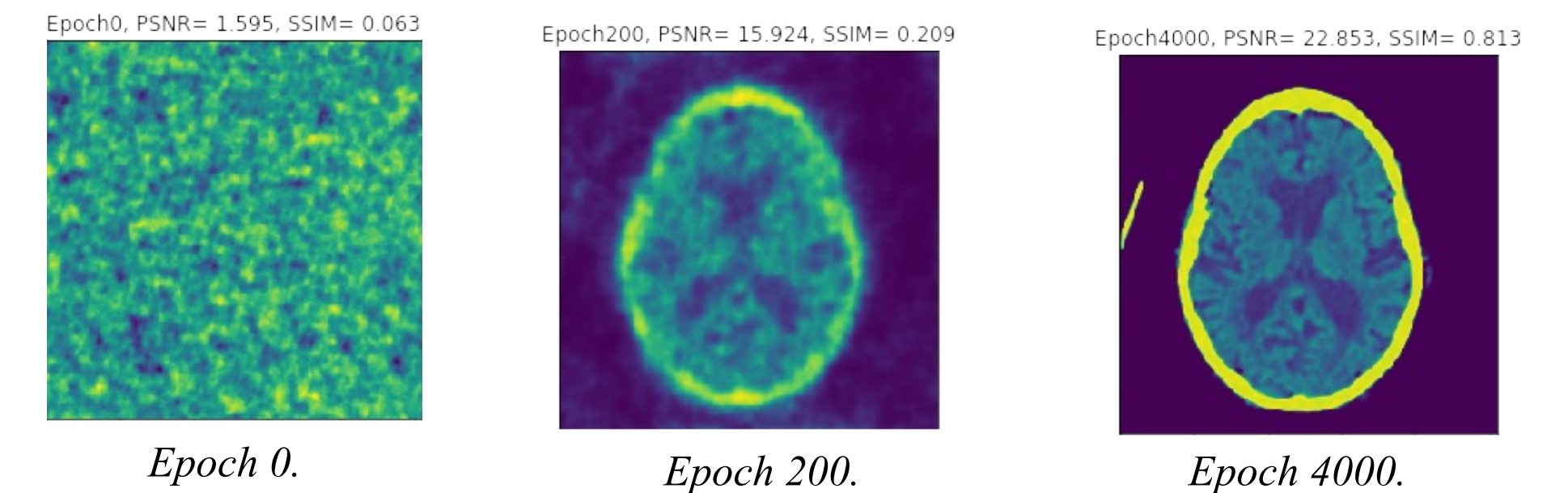


Figure 5. Reconstructed CT images from our proposed pipeline with 200 sinogram pixels/iteration. Images shown are from epoch 0, 200, and 400. The ground truth CT image and sinogram are shown in figure 1.

Conclusion and Future Work

- Our proposed method has enabled high-resolution computed tomography representations in neural networks with conventional GPUs.
- The method is yet to be expanded to 3-D where more applied problems can be addressed.
- The ray (sinogram pixels) sampling method (random vs non-random) is still being evaluated.
- Additional priors can be incorporated to study their effects on the reconstruction quality.

Acknowledgement

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References

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- [2] "Radon Transform." Wikipedia, 8 June 2021, en.wikipedia.org/wiki/Radon_transform. Accessed 11 April 2022.